Name:

All technology (phone, calculator, anything that has a computer) should be stored in your bag during the quiz.

1. (Reviewing vocabulary) Let f be a function and let a be a real number. According to Stewart's definition, f is called *continuous* at a if:

i. f(a) is ______ ,

ii. ______ exists, and

iii. f(a) =_____.

Answer: See Sec 2.5 *Continuity* pages 115-117 def 1 and 3.

- 2. (Reviewing vocabulary) Let f be a function that is defined on $(-\infty, \infty)$.
 - i. According to Stewart's definition, writing

$$\lim_{x \to \infty} f(x) = 50$$

means that

Answer: See Sec 2.6 Limits at Infinity page 127.

ii. In this situation, does the limit of f(x) (as x increases without bound) exist?

- 3. (Reviewing vocabulary) Let f be a function that is defined on $(-\infty, \infty)$.
 - i. According to Stewart's definition, writing

$$\lim_{x \to \infty} f(x) = \infty$$

means that

ii. In this situation, does the limit of f(x) (as x increases without bound) exist?

Answer: See Sec 2.6 page 137 for definition of an "infinite limit" at infinity.

- 4. (a) What is a sequence?
 - (b) Let $\{b_n\}$ be a sequence. What does it mean to write $\lim_{n \to \infty} b_n = 7$?

(c) Let $\{b_n\}$ be a sequence. What does it mean to write $\lim_{n \to \infty} b_n = \infty$?

Answer: See the back-of-the-book answer for Sec 11.1 Sequences p1(a)-(c) on page 704.

- 5. (a) What is a convergent sequence? Give two examples.
 - (b) What is a divergent sequence? Give two examples.

Answer: See Examples 4 through 11 in Sec 11.1 Sequences pages 698–700

- 6. (Optional, for extra practice). WebAssign questions on sequence recognition Sec 11.1 (access via HuskyCT). Everyone automatically gets a 2-week (or sometimes one month) free trial of WebAssign.
- 7. (More textbook problems) Sec 11.1 Example 2, Sec 11.1 problems 23, 41, 47, 55, Sec 11.1 problems 65, 69, 71.
- 8. (Sequence recognition) For each part, (i) find a non-recursive formula for the *n*th term in the sequence. (ii) Describe the end behavior of this sequence. (iii) If the sequence is convergent, compute or guess its limit explain (in words or using math symbols) how you get this number (no formal proof is needed).
 - (a) $\{5, -5, 5, -5, 5, \dots\}$
 - (b) $\{5, 8, 11, 14, 17, \dots\}$

(c)
$$\left\{-3, 2, -\frac{4}{3}, \frac{8}{9}, -\frac{16}{27}, \dots\right\}$$

(d) More sequence recognition problems on the textbook are Sec 11.1 Sequences problems 13 - 18.

Hint: You can check your work against the computer sequence recognition, for example, using software like WolframAlpha: https://www.wolframalpha.com/examples/mathematics/discrete-mathematics/sequences/

9. (Vocabulary) (Note: \mathbb{R} is the notation for the set of all real numbers.) Let $f : \mathbb{R} \to \mathbb{R}$ be the function defined by

$$f(x) = \frac{16x^2 - 8x - 6}{18x^2 - 6x + 8}$$

By applying L'Hospital's Rule (see Sec 4.4 page 305) twice, we get

$$\lim_{x \to \infty} f(x) = \frac{16}{18}.$$
 (1)

Due to a theorem (Thm 3, page 697) explained in Sec 11.1 of Stewart, we can use equation (1) to show that the sequence $\{a_n\}$ defined by

$$a_n = \frac{16n^2 - 8n - 6}{18n^2 - 6n + 8}$$

also converges to $\frac{16}{18}$, or, in notation form,

$$\lim_{n \to \infty} a_n = \frac{16}{18}.\tag{2}$$

What does (2) mean (according to the definition of limit of a sequence)?