

**Useful trig facts.**

$$\sin^2 \theta + \cos^2 \theta = 1, \quad \tan^2 \theta + 1 = \sec^2 \theta, \quad \cos^2 \theta = \frac{1}{2}(1 + \cos 2\theta), \quad \sin^2 \theta = \frac{1}{2}(1 - \cos 2\theta)$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta, \quad \sin 2\theta = 2 \sin \theta \cos \theta$$

$$\sin \frac{\pi}{6} = \frac{1}{2}, \quad \sin \frac{\pi}{3} = \frac{\sqrt{3}}{2}, \quad \sin \frac{\pi}{4} = \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}, \quad \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}, \quad \cos \frac{\pi}{3} = \frac{1}{2},$$

**Some derivatives and antiderivatives.**

$$\frac{d}{dx} \sin(x) = \cos(x)$$

$$\frac{d}{dx} \cos(x) = -\sin(x)$$

$$\frac{d}{dx} \tan(x) = (\sec(x))^2$$

$$\frac{d}{dx} \csc(x) = -\csc(x) \cot(x)$$

$$\frac{d}{dx} \sec(x) = \sec(x) \tan(x)$$

$$\frac{d}{dx} \cot(x) = -(\csc(x))^2$$

$$\frac{d}{dx} \arcsin(x) = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \arccos(x) = \frac{-1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx} \arctan(x) = \frac{1}{1+x^2}$$

$$\frac{d}{dx} b^x = \ln(b) b^x$$

$$\int \sec x \, dx = \ln |\sec x + \tan x| + C. \quad \int \frac{dx}{x^2+a^2} = \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C \text{ if } a \neq 0.$$

**Fundamental Theorem of Calculus, part I.**

Part 1: If  $f$  is continuous on  $[a, b]$ , then function  $g$  defined as

$$g(x) = \int_a^x f(t) \, dt, \quad a \leq x \leq b$$

satisfies  $g'(x) = f(x)$ .

**Fundamental Theorem of Calculus, part II.**

If  $f$  is continuous on  $[a, b]$ , then

$$\int_a^b f(x) \, dx = F(b) - F(a)$$

where  $F$  is any anti-derivative of  $f$  (ie.  $F$  is any function such that  $F' = f$ ).

**Restricted domains for trig functions**

$$\sin \theta \text{ for } -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$$

$$\cos \theta \text{ for } 0 \leq \theta \leq \pi$$

$$\tan \theta \text{ for } -\frac{\pi}{2} < \theta < \frac{\pi}{2}$$

$$\csc \theta \text{ for } \theta \text{ in } [-\pi/2, 0) \cup (0, \pi/2]$$

$$\sec \theta \text{ for } \theta \text{ in } [0, \pi/2) \cup (\pi/2, \pi]$$

$$\cot \theta \text{ for } 0 < \theta < \pi$$

**Partial Fraction Decomposition.**

$$\frac{1}{(x-a)(x-b)} = \frac{A}{x-a} + \frac{B}{x-b} \text{ if } a \neq b, \text{ and}$$

$$\frac{1}{x(x^2+a)} = \frac{A}{x} + \frac{Bx+C}{x^2+a} \text{ if } a \neq 0$$