Section 10.3 Part 1

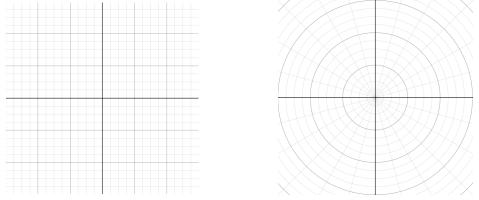
Polar Coordinates

Intuition (Euler Formula):

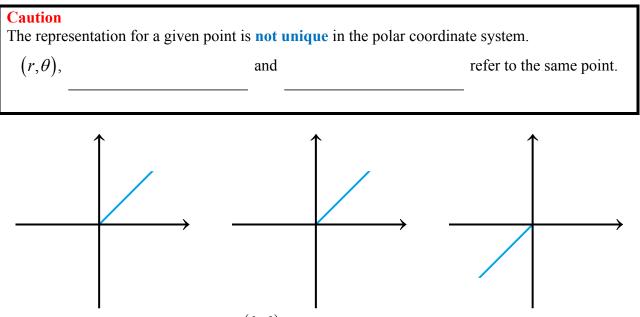
Polar Coordinates

(In Multivariable Calculus: polar coordinates \rightarrow cylindrical and spherical coordinates in 3D)

Instead of using **horizontal distance** and **vertical distance** from the axes, we use the distance from the origin (**radius**) as well as the corresponding **angle** to express a given point.



The origin is called the **pole**, and the positive x-axis is called the **polar axis**. The polar coordinates for a point P have the form (r, θ) , where the **radial coordinate** r describes the distance from the origin to P, and the **angular coordinate** θ describes an angle starting from the positive x-axis and ending on the ray that passes through the origin and P. As usual, positive angles are measured **counterclockwise** from the positive x-axis.



The origin is specified as $(0, \theta)$ in polar coordinates, where θ is any angle.

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Example:

Graph the point $\left(1, \frac{5\pi}{4}\right)$ in polar coordinates. Give two alternative representations for the point.

Converting Between Cartesian and Polar Coordinates

Procedure Converting Coordinates

A point with polar coordinates (r, θ) has Cartesian coordinates (x, y), where

A point with Cartesian coordinates (x, y) has polar coordinates (r, θ) , where

Example:

Express the point with polar coordinates $\left(2, \frac{3\pi}{4}\right)$ in Cartesian coordinates.

Example:

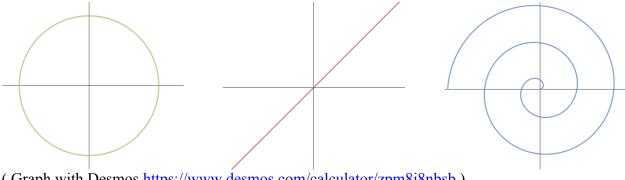
Express the point with Cartesian coordinates (1, -1) in polar coordinates.

Converting Between Cartesian and Polar Equations

A curve in polar coordinates is the set of points that satisfy an equation in r and θ . Some sets of points are easier to describe in polar coordinates than in Cartesian coordinates.

For example,

- The polar equation r = 3.
- The polar equation $\theta = \frac{\pi}{4}$.
- The polar equation $r = \theta$.



(Graph with Desmos https://www.desmos.com/calculator/zpm8i8nbsb)

Example:

Convert the polar equation $r \cos \theta = -4$ to Cartesian equations.

Example: Convert the polar equation $r = 8\sin\theta$ to Cartesian equations. Section 10.3 Part 1

Graphing in Polar Coordinates

Example:

Graph the polar equation $r = 1 + \sin \theta$.

