You are encouraged to discuss your work with your classmates but this assignment is to be completed individually (that is, don't share/ let someone take a picture of your full solutions). Solutions must be written on separate paper(s) with each problem clearly marked. Show all work neatly and give thoughtful explanations where necessary.

1. (Credit) Please give credit to people who worked with you (including the people that you helped and the people who gave you help), any textbooks or notes you used (other than Stewart), and the website addresses of any internet resources you might have used (other than WebAssign).
2. (Style points) You will earn full "Style points" if each of your solution is legible, coherent, and not ambiguous. In addition, your reader should not need to reread your solution several times to find a train of thought. One tip is that your final draft should not include any scratch work. (I expect almost everyone to receive full points on this - you can show me a sample of your work before the due date if you are not sure).
3. (Key words: vocabulary, Sec 2.5 , continuity, interval)
(a) (page 115) Let $f$ be a function and let $r$ be a real number. According to Stewart's definition, $f$ is called continuous at $r$ if: $f(r)$ is $\qquad$ exists, and $f(r)=$ $\qquad$
Warning: a function does not need a derivative at $r$ to be continuous at $r$.
(b) (page 117) Let $I$ be the open interval ( $a, b$ ), that is, $\{x$ is a real number: $a<x<b\}$. What does it mean for $f$ to be continuous on the interval $I$ ?
4. (Key words: vocabulary, limits and sequences, convergent series)
(a) (Sec 11.1 page 696) Let $\left\{a_{n}\right\}$ be a sequence and let $L \in \mathbb{R}$ (this notation means that $L$ is a real number). What does $\lim _{n \rightarrow \infty} a_{n}=L$ mean? Warning: do not include variations of the words "converge", "diverge", "approach", or "infinity" in your answer. Another warning: in general $\lim _{n \rightarrow \infty} a_{n}=L$ does NOT imply that " $a_{n}$ will never reach $L$ ".
(b) (Sec 11.1 page 697) What does it mean to write $\lim _{n \rightarrow \infty} b_{n}=\infty$ ? Warning: do not include variations of the words "converge", "diverge", "approach", "increase", "continuously", or "infinity" in your answer.
(c) (Sec 11.2, page 708) Let $\left\{c_{n}\right\}$ be a sequence. What is a partial sum of $\left\{c_{n}\right\}$ ?
(d) (Sec 11.2, page 708) Let $\left\{c_{n}\right\}_{n=1}^{\infty}$ be a sequence. We say that the infinite series $\sum_{n=1}^{\infty} c_{n}$ is convergent if
 is not convergent or divergent.
5. (Key words: Sec 11.1, monotonic sequence theorem, page 702) Either give an example of a sequence satisfying the condition (no explanation necessary) or explain why no such sequence exists.
(a) A monotonically decreasing sequence that converges to 10 .
(b) A monotonically increasing bounded sequence that does not converge (that is, diverges).
(c) A non-monotonic sequence that converges to $\frac{3}{4}$.
6. (Key words: Sec 11.1, precise definition) Each of the following series $a_{n}$ converges to a limit $L$. For $\epsilon=\frac{1}{100}$, find $a$ positive number $N$ such that, if $n>N$, then $a_{n}$ is within distance $\epsilon$ of $L$. Then for an arbitrarily small $\epsilon$, find an $N$. SEE EXAMPLE https://egunawan.github.io/fall17/notes/notes11_1choosingN.pdf
(a) $a_{n}=\frac{1}{n^{2}+3}, L=0$.
(b) $a_{n}=\frac{3 n+2}{2 n-1}, L=\frac{3}{2}$.
(c) $a_{n}=\frac{n^{2}+2}{n^{2}-3}, L=1$.
7. (Key words: Sec 11.1, sequence, squeeze theorem) The sequence $a_{n}=(5 n+4) /\left(3 n^{2}-2\right)$ converges to 0 . Justify this fact by squeezing $a_{n}$ between 0 and another sequence of type $b_{n}=$ (some constant) $/ n$ and using the Squeeze theorem. You may assume that $\lim _{n \rightarrow \infty}($ any constant $) / n=0$.
See a similar (model) solution at: https://egunawan.github.io/fall17/hw/models.pdf
8. (Key words: Sec 11.2 series, decimal expansion)
(a) Use geometric series to write $2.74 \overline{9}=2.74999999 \ldots$ as a fraction.
(b) Write a different decimal expansion for $2.74999999 \ldots$ (Hint: can you use your solution above?)
(c) i. Find the (exact, not rounded up) repeating decimal expansions of $\frac{1}{7}, \frac{2}{7}, \frac{3}{7}, \frac{4}{7}, \frac{5}{7}$, and $\frac{6}{7}$. You should practice doing at least two of them without the help of a computer (hint: do long division) so that you can do this on a test, but you don't need to include it in your submission.
ii. List them in a table and note the interesting pattern.
iii. Choose just ONE the six fractions above and show that your repeating decimal expansion is indeed the same as the fraction. If you don't enjoy working with many digits, you can use a computing tool - make sure it gives you exact fractions (for example, WolframAlpha would work).
9. (Key words: Sec 11.2 series) Do just ONE of the following:

Option I: There is a famous set $C$ which is formed by repeating the following process infinitely many times. Start with the interval $C_{0}=[0,1]=\{x$ a real number : $0 \leq x \leq 1\}$. Remove the open middle third of this interval. Now you are left with $C_{1}=[0,1 / 3] \cup[2 / 3,1]$. Next, remove the open middle thirds of each of the remaining intervals, i.e. remove $(1 / 9,2 / 9)$ and $(7 / 9,8 / 9)$. You are left with $C_{2}=[0,1 / 9] \cup[2 / 9,1 / 3] \cup$ $[2 / 3,7 / 9] \cup[8 / 9,1]$.
(a) Draw a separate number line representing each of $C_{0}, C_{1}, C_{2}$ and $C_{3}$. It will help you visualize what is going on if you draw the number line for $C_{1}$ below the number line for $C_{0}$ and so on.
(b) What are the lengths of $C_{0}, C_{1}, C_{2}$ and $C_{3}$ ?
(c) Find an expression for the length of $C_{n}$.
(d) What are the lengths of the $C$ ? (Hint: use geometric series)
(e) Is $C$ empty? If not, list some numbers that belong to $C$. Explain.

Option II: A two-dimensional counterpart of the above famous set is a 'carpet' square $S$ which is formed by repeating the following process infinitely many times. Start with a filled square of side 1 , call it $S_{0}$. Remove the center square (of side $1 / 3$ ) of the original square and now you are left with $S_{1}$. Then remove the center squares (of side $1 / 9$ ) of the eight smaller remaining squares to get $S_{2}$, and so on.
(a) Sketch $S_{0}, S_{1}$, and $S_{2}$ on the $x-y$ coordinate plane. Sketching $S_{3}$ is optional (lots of missing squares) but may be helpful.
(b) What are the areas of $S_{0}, S_{1}, S_{2}$ and $S_{3}$ ?
(c) Find an expression for the area of $S_{n}$.
(d) What is the area of the $S$ ? (Hint: use geometric series)
(e) Is $S$ empty? If not, list some points that belongs to $S$. Explain.
10. (Write your own problem) Review the topics of Sec 11.1 and Sec 11.2.
(a) Write a (non-vocabulary) problem that you think requires a decent understanding of one or more of the concepts/ skills to solve. (For ideas, you may look at Stewart's textbook or other textbooks or WebAssign, but don't just copy the problem). The problem's solution should require more than simply writing down a definition from the textbook.
(b) Explain briefly why you chose to highlight certain concepts (for example, maybe you think it's interesting, difficult, or has applications to science).
(c) Write a complete solution to your problem.
(d) Show your problem to your classmates to get their feedback. Write a brief, one-sentence comment about what other people thought. One or two questions submitted from students may be chosen for future test questions.

