There are partial solutions to some of Gallian textbook exercises, at the back of the book.

## 1. From the textbook

- (1) Read Gallian Chapter 7 pg 138-140 (including Examples 1, 2, 3, and the 9-item lemma). Then paraphrase the last paragraph of page 140.
- (2) Do Gallian Textbook Chapter 7 Exercise 1 (pg 150).
- (3) Do Gallian Textbook Chapter 7 Exercise 2 (pg 150).
- (4) Do Gallian Textbook Chapter 7 Exercise 3 (pg 150).
- (5) Read Gallian Chapter 7 Example 4 (pg 141). Then do a similar computation: Gallian Textbook Chapter 7 Exercise 5 (pg 150).
- (6) Paraphrase (or copy word-for-word):
  - Chapter 7 Theorem 7.1 (Lagrange's Theorem) and its proof (pg 142).
  - Chapter 7 Corollaries 1, 2, 3 and their proofs (pg 143).

## 2. Coset properties

**Theorem 1.** Suppose H is a subgroup of a group G, and  $a, b \in G$ . Then the following conditions are equivalent.

- (i) aH = bH
- (ii)  $aH \subset bH$
- (iii)  $b \in aH$
- (iv)  $a^{-1}b \in H$

The already-typed proofs in Typesetting Project 05 show that (ii) implies (i) and also that (iv) implies (iii), and your Overleaf assignment was to type a proof showing (iii) implies (ii). To complete the proof of this theorem, we only need to show (i) implies (iv).

Your homework problem: Prove that (i) implies (iv). Suppose aH = bH. Prove that  $a^{-1}b \in H$ .